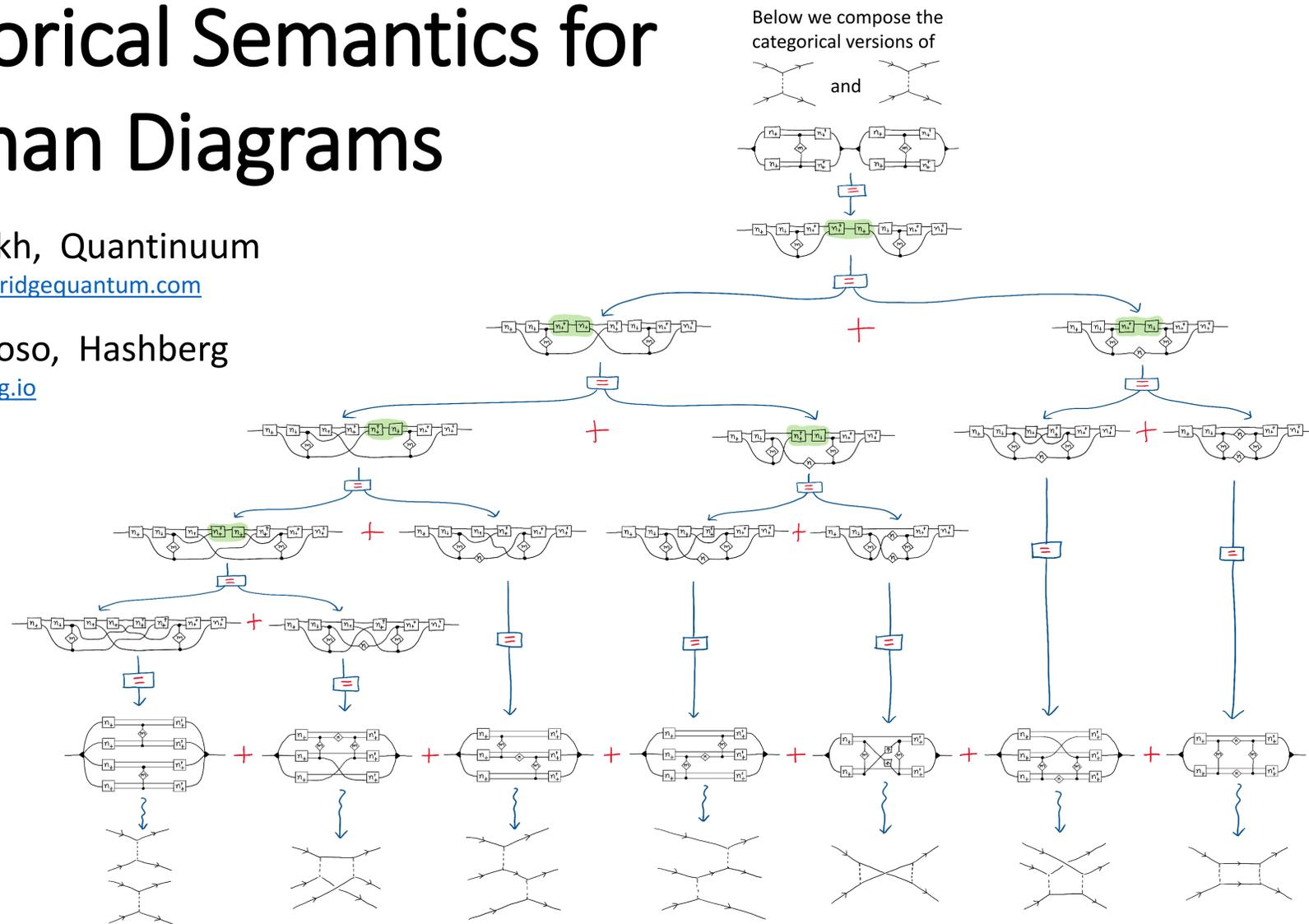


# Categorical Semantics for Feynman Diagrams

Razin A. Shaikh, Quantinuum  
[razin.shaikh@cambridgequantum.com](mailto:razin.shaikh@cambridgequantum.com)

Stefano Gogioso, Hashberg  
[quantum@hashberg.io](mailto:quantum@hashberg.io)



Sequential composition of two categorical Feynman diagrams results in the superposition of all possible graph-theoretic combinations of the individual diagrams

Examples	
nucleon – nucleon scattering (2 <sup>nd</sup> order)	
nucleon – nucleon scattering (4 <sup>th</sup> order)	
nucleon – anti-nucleon scattering	
meson decay	
meson – meson scattering	

### Ingredients

- Creation and annihilation operators
- Feynman propagator
- Split and merge maps

### Rules

- Isometry
- Sliding rule (split)
- Sliding rule (merge)

### Categorical Feynman Diagrams

For a given Feynman diagram, we consider its corresponding term in Wick's expansion. We translate that term into a string diagram, obtaining a linearized version of the Feynman diagram as a process in our  $\star$ Hilb category.

We rewrite the string diagram using the given rules to obtain the categorical Feynman diagram.

introduce a split-merge pair      sliding rules      replace sums with spiders      fuse spiders